

# The Golem Group/University of California at Los Angeles Autonomous Ground Vehicle in the DARPA Grand Challenge

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This paper presents the Golem Group/University of California at Los Angeles entry to the 2005 DARPA Grand Challenge competition. We describe the main design principles behind the development of Golem 2, the race vehicle. The subsystems devoted to obstacle detection, avoidance, and state estimation are discussed in more detail. An overview of vehicle performance in the field is provided, including successes together with an analysis of the reasons leading to failures. © 2006 Wiley Periodicals, Inc.

## 1. OVERVIEW

The Golem Group is an independent team of engineers formed to build a vehicle for the 2004 DARPA Grand Challenge (DGC). For the 2005 DARPA Grand Challenge, the Golem Group and the University of California at Los Angeles (UCLA's) Henry Samueli School of Engineering and Applied Science joined forces to build a second autonomous vehicle, Golem 2 (see Figure 1). Performance highlights of this vehicle are summarized in Table I.

The aspect of the DGC was to require high-speed autonomous driving in the unstructured or semi-structured environment typical of rough desert trails. Global positioning system (GPS) waypoint following was necessary, but not sufficient, to traverse the route,

which might be partially obstructed by various obstacles. In order to have a good chance of completing the course, vehicles needed to drive much faster, yet have a lower failure rate, than previously achieved in an off-road environment without predictable cues. High-speed driving over rough ground posed a vibration problem for sensors.

### 1.1. Relation to Previous Work

Prior to the DGC, unmanned ground vehicles had driven at very high speeds in structured paved environments (Dickmanns, 1997, 2004). Other vehicles had operated autonomously in unstructured off-road environments, but generally not at very high speed. Autonomous Humvees using ladar (laser de-



**Figure 1.** Golem 2 driving autonomously at 30 miles per hour.



**Figure 2.** Golem 1 negotiating a gated crossing in the 2004 DARPA Grand Challenge. (Photos courtesy of DARPA.)

tection and ranging) to detect obstacles in an off-road environment have been developed at the National Institute for Standards and Technology (Coombs, Murphy, Lacaze & Legowik, 2000; Hong, Shneier, Rasmussen & Chang, 2002). The U.S. Army Experimental Unmanned Vehicle (Bornstein & Shoemaker, 2003) also used ladar to detect obstacles and could navigate unstructured rough ground at somewhat over 6 km/h. Rasmussen (2002) used a combination of ladar and vision to sense obstacles and paths in off-road environments. The Carnegie Mellon University (CMU) Robotics Institute had perhaps the most successful and best-documented effort in the first DGC, building an autonomous Humvee which was guided by ladar (Urmson, 2005; Urmson et al., 2004).

Golem 1, our own first DGC entry, used a single laser scanner for obstacle avoidance. Golem 1 traveled 5.1 miles in the 2004 Challenge (see Figure 2), before stopping on a steep slope because of an excessively conservative safety limit on the throttle control. This was the fourth-greatest distance traveled in the 2004 DGC; a good performance considering Golem 1's small total budget of \$35,000.

Our attempts to improve on the performance of previous researchers were centered on simplified streamlined design—initially in order to conserve costs, but also to enable faster driving by avoiding computational bottlenecks. For example, we relied

**Table 1.** Golem Group/UCLA performance in the 2005 DARPA Grand Challenge. NQE=National Qualifying Event; GCE=Grand Challenge Event; CMU=Carnegie Mellon University; IVST=Intelligent Vehicle Safety Technologies.

NQE Performance Highlights	
9 min 32 s NQE run clearing 49/50 gates and 4/4 obstacles	Only Stanford, CMU, and IVST made faster runs clearing all obstacles Only Stanford and CMU made faster runs clearing at least 49 gates
12 min 19 s NQE run clearing 50/50 gates and 5/5 obstacles	Only Stanford, CMU, Princeton, and Cornell made faster flawless runs
GCE Performance Highlights	
Peak speed (controlled driving) 47 mph Completed 22 race miles in 59 min 28 s Anecdotally said to be fastest vehicle reaching 16-mile DARPA checkpoint Crash after 22 miles due to memory management failure	

primarily on ladar for obstacle avoidance, but unlike the majority of ladar users, we did not attempt to build a three-dimensional (3D) model of the world *per se*. Instead, we only attempted to detect the most important terrain features and track the locations of those on a two-dimensional (2D) map. Golem 1, with its single ladar scanner, may have gone too far in the direction of simplicity, and Golem 2 carried multiple ladars to better distinguish slopes and hill-sides. Ladar obstacle detection is further discussed in Section 3.

As another example of simplification, our path planning process considers possible trajectories of the truck as simple smooth curves in the 2D plane, with curvature of the trajectory as a measure of drivability, and distance to the curve as a proxy for danger of collision. We do not consider obstacles in a configuration space of three dimensions, much less six dimensions. Our approach might be inadequate for navigating a wholly general mazelike environment, but more importantly, for our purposes, it gives fast results in the semistructured case of a partially obstructed dirt road. Trajectory planning is discussed further in Section 4.

We did experiment with some vision systems in addition to ladar. Mobileye Vision Technologies, Ltd. provided Golem 2 with a monocular roadfinding system, which is discussed in Section 6.1 and also in Alon, Ferencz & Shashua (2006). This could be considered as extending the cue-based paved-environment work of Dickmanns, and of Mobileye, to an unpaved environment. Experiments with a Toshiba stereo vision system are described in Section 6.2.

## 2. VEHICLE DESIGN

Each of our vehicles was a commercially available pickup truck, fitted with electrically actuated steering and throttle, and pneumatically actuated brakes.

We felt it was very important that the robot remained fully functional as a human-drivable vehicle. Golem 1 seats two people while Golem 2 seats up to five. A passenger operated the computer and was responsible for testing, while the driver was responsible for keeping the vehicle under control and staying aware of the environment. During testing, it was very convenient to fluidly transition back and forth between autonomous and human control. Individual actuators (brake, accelerator, and steering) can be en-

abled and disabled independently, allowing isolation of a specific problem. Having a human “safety driver” increased the range of testing scenarios that we were willing to consider. Finally, having a street-legal vehicle greatly simplified the logistics.

Accordingly, a central principle behind actuation was to leave the original controls intact, to as great an extent as possible, in order to keep the vehicle street legal. The steering servo had a clutch, which was engaged by a pushrod that could be reached from the driver’s seat. The brakes were actuated by a pneumatic cylinder that pulled on a cable attached—through the firewall—to the back of the brake pedal. The cable was flexible enough to allow the driver to apply the brakes at any time. The pressure in the cylinder could be continuously controlled via a voltage-controlled regulator. A servo was attached directly to the steering column.

A second design aim was to keep the computational architecture as simple as possible. The core tasks of autonomous driving do not require a large amount of computational power. We worked to keep the software running on a single laptop computer. Unburdened by a rack full of computers, we were able to retain working space in the vehicle, but more importantly, any team member could plug in their laptop with a universal serial bus (USB) cable and run the vehicle. A block diagram of the architecture is shown in Figure 3.

### 2.1. Sensors

The sensors mounted on Golem 2 for vehicle state estimation included a Novatel ProPak LB-Plus differential GPS receiver with nominal 14-cm accuracy using OmniStar HP correction; a BEI C-MIGITS inertial measurement unit (IMU); a custom Hall encoder on the differential for odometry with approximately 10-cm accuracy; and a 12-bit encoder for measuring the steering angle. Vehicle state estimation is discussed further in Section 5.

The sensors used for terrain perception included a Sick LMS-221 ladar, which swept a 180° arc in front of the vehicle—measuring ranges up to 80 m at 361 samples/sweep, 37.5 sweeps/s, with the samples interleaved 0.5° apart. There were also four Sick LMS-291 ladars, similar in most respects except that they each swept a 90° arc while collecting 181 samples/sweep, 75 sweeps/s. The arrangement and function of the ladars is further discussed in Section 3. A monocular camera system from Mobileye, used for road

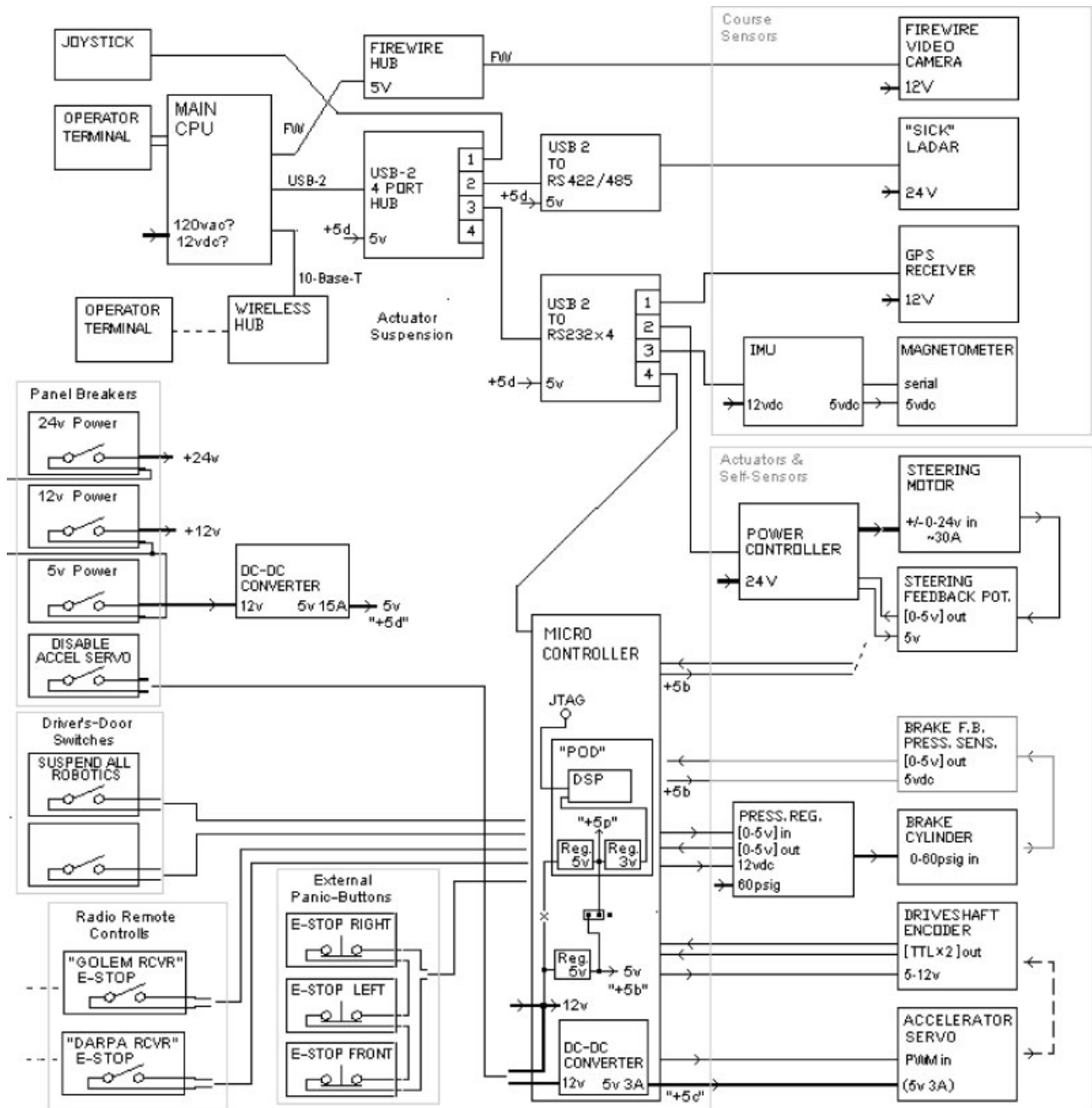


Figure 3. Block diagram of the Golem vehicle architecture.

finding, was mounted at the "hood ornament" position, while a stereo system from Toshiba looked out through the windshield.

The On-Board Diagnostics Bus II provided limited access to vehicle data; it was mainly used to control the vehicle's horn.

## 2.2. Software

In order for multiple developers to work in parallel, it was plain that we needed a system which would give us the freedom to write code in diverse places, such as deserts and stadium parking lots, while still

maintaining all features of a revision control system. We found this in the peer-to-peer revision control system, *darcs* (Roundy, 2005), which maintains repositories containing both the source code and a complete history of changes, and allows a developer to push or pull individual patches from one source repository to another. Using *darcs*, we achieved a very tight development-test cycle despite our diverse working environments.

The software ran on a Linux laptop and was divided into two main applications. The program which made decisions based on sensor input, controlled the actuators, and recorded events is known as *golem*. It had no connection to the visualization software *dashboard*, other than through the log files it created, which were human-readable plain text. Besides being written to disk, these log files could be piped directly from *golem* to *dashboard*, for realtime visualization or replayed offline by *dashboard* at a later time.

Commands could be typed directly to *golem* at the console or received from *dashboard* over a user datagram protocol (UDP) port. The commands were designed to be simple and easily typed while driving in a moving vehicle on a dirt road. While this was convenient, it might have been even more convenient to be able to use an analog control, or at least the arrow keys, to adjust control parameters in real time.

### 2.2.1. Golem

The main software for data capture, planning, and control, *golem* consisted of two threads. The main thread was completely reactionary and expected to be real time; it took in data from the sensors, processed them immediately, and sent commands to the actuators. The low-level drivers, the state estimators, ladar and obstacle filters, the road/path follower, the velocity profiler, and the controllers all ran in this thread. A second planning thread was allowed to take more time to come up with globally sensible paths for the vehicle, based on snapshots of the accumulated sensor data received at the time the thread was initiated.

*Golem* could be driven by real-time sensor data, by a simple simulator, or from previously recorded log data. The simulator was invaluable for debugging the high-level behaviors of the planner, but its models were not accurate enough to tune the low-level controllers. The replay mode allowed us to de-

bug the ladar obstacle filters and the state estimators in a repeatable way, without having to drive the vehicle over and over.

### 2.2.2. Dashboard

*Dashboard* was created from scratch using C, Gtk+2, and OpenGL, to be an extensible visualization tool which would allow us to play back our log files and learn from their content. A typical screenshot is shown in Figure 4.

The core of *dashboard* consists of a log file parsing library, an OpenGL representation of the world, and a replaying mechanism which controls the flow of time. *Dashboard* takes a log file from disk, standard input, or a UDP network connection, as input, and uses rules described in a configuration file to convert human-readable log lines into an internal representation that is easy for other program components to index and access. Log lines are parsed as soon as they are available, by the Perl compatible regular expression library. The internal representation is displayed for the user through the OpenGL window. The user has the ability to play log files, pause them, rewind, fastforward, measure and move around in the rendered world, and selectively view sensor visualizations of interest. This proved indispensable in our development effort.

The data are visualized in a number of different ways, as we found that no one representation was suitable for all debugging situations. The main section is a graphical representation of the world which is viewable from a 2D top-down point of view and also from a 3D point of view. It is rendered using OpenGL. There is also a section that displays inputs as textual data for precise readings. Yet another section contains a set of user programmable graphs. Because of the intentionally generic internal representation, adding a new element to the visualization, such as data from a new sensor, is a very simple process.

## 3. LADAR OBSTACLE DETECTION

We considered a nontraversable obstacle to be an object or ground feature which: (a) Represented a rapid apparent change in ground elevation, with a slope magnitude greater than 30°, or an actual discontinuity in ground surface; (b) presented a total change in ground height too large for the vehicle to simply roll





Figure 4. Dashboard visualization of Golem 2 entering a tunnel during an NQE run.

over; and (c), if discontinuous with the ground, was not high enough for the vehicle to pass under. This was an adequate definition of an “obstacle” for the DARPA Grand Challenge.<sup>1</sup> Since obstacles result from changes in ground elevation, the most critical information comes from comparisons of surface measurements adjacent in space.

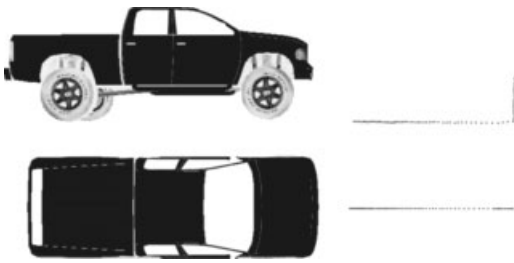
We did not use sensor data integrated over time to build a map of absolute ground elevation in the world frame, on the hypothesis that this is unnecessarily one step removed from the real information of interest. Instead, we tried to directly perceive, or in-

<sup>1</sup>Ideally, one would like to classify some objects, such as plants, as “soft obstacles” that can be driven over even if they appear to have steep sides. Other hazards, such as water or marshy ground, cannot be classified simply as changes in ground elevation. But this increased level of sophistication was not necessary to complete the DGC and remains a topic of future work for us.

fer, from instantaneous sensor data, regions of rapid change in ground elevation in the body-fixed frame, and then maintain a map of those regions in the world frame. We did not concern ourselves with any ground slope or surface roughness that did not rise to the threshold of making the ground nontraversable.

### 3.1. Ladar Geometry

We used Sick LMS-291 and LMS-221 laser scanners as our primary means of obstacle detection. It is interesting that the many DGC teams using 2D ladars, such as these, found a wide variety of ways of arranging them. These ladars sweep a rangefinding laser beam through a sector of a plane, while the plane itself can be rotated or translated, either by vehicle motion or by actuating the ladar mount. The choice



**Figure 5.** Returns from a ladar oriented in a vertical plane.

of plane or, more generally, the choice of scan pattern for any beam-based sensor, represents a choice between scanning rapidly in the azimuthal direction, with slower or sparser sampling at different elevation angles, or the reverse.

A ladar scanning in the vertical plane has the significant advantage that the traversability of the scanned terrain is apparent from a single laser sweep. For example, it is easily determined from the single vertical-plane scan in Figure 5 that the ground is continuous, flat, and traversable from a few feet before the truck, up to the point where there is a nontraversable vertical surface taller than the vehicle's wheels.

In our case, a single-laser sweep takes  $1/75$  s and individual sample points are separated by  $1/13,575$  s. On this time scale, it is not likely that motion or vibration of the vehicle could distort the vertical scan sufficiently to alter this interpretation (make the traversable ground appear nontraversable or vice versa). Similarly, while small errors in the estimated pitch of the vehicle would induce small errors in the estimated location of the nontraversable obstacle, it is not likely that they could cause a major error or prevent the perception of an obstacle in the right approximate location. Against these advantages is the obvious drawback that a vertical slice only measures the terrain in a single-narrow direction. Even if there are multiple vertical scanners and/or the vertical plane can be turned in different directions, the vehicle is likely to have a blinkered view with sparse azimuthal coverage of the terrain, and may miss narrow obstacles.

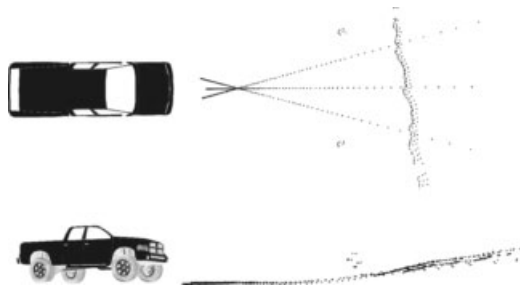
Conversely, a scan plane which is horizontal, or nearly, horizontal, will provide good azimuthal coverage, and clearly show narrow obstacles, such as fenceposts and pedestrians, but the interpretation of

any single-horizontal scan in isolation is problematic. Lacking measurements at adjacent elevation angles, one cannot determine if a return from a single-horizontal scan is from a nontraversable steep surface or from a traversable gently sloping one. Therefore, the information from multiple horizontal scans must be combined; but since the crucial comparisons are now between individual measurements taken at least  $1/75$  s apart instead of  $1/13,575$  s apart, there is a greater likelihood that imperfectly estimated motion or vibration will distort the data. Small errors in pitch, roll, or altitude could cause the vehicle to misapprehend the height of a ground contour and lead to a totally erroneous classification of the terrain as traversable or nontraversable.

Our approach was to use a complementary arrangement of both vertical and nearly horizontal ladars. On the Golem 2 vehicle, there are two nearly horizontal ladars and three vertically oriented ladars mounted on the front bumper. The idea is that the vertically oriented ladars are used to form a profile of the general ground surface in front of the truck, in the truck body-fixed frame (as opposed to a world-fixed frame). The ground model we fit to the data was piece-wise linear in the truck's direction of motion, and piece-wise constant in the sideways direction. The model interpolated the most recent available ladar data. In locations beyond the available data, the ground was assumed to have constant altitude in the body-fixed frame.

The apparent altitude of returns, from the nearly horizontal ladars relative to the ground model, was then computed to see if those returns were: (a) Consistent with a traversable part of the ground model; (b) consistent with a nontraversable part of the ground model; (c) apparently from an elevation moderately higher than the notional ground; or (d) apparently from an object so far above the notional ground that the vehicle should be able to pass under it. In either Case (b) or (c), the ladar return is classified as arising from a possible obstacle; after several of these returns are received from the same location at different vantage points, the presence of an obstacle is confirmed. In practice, an object, such as a parked car, will be represented as a cluster of adjacent obstacles.

For example, Figure 6 illustrates ladar data from a portion of the NQE course. The returns from the horizontally oriented ladars indicated a long straight feature crossing in front of the vehicle, and two smaller features, or clusters, of returns. The three



**Figure 6.** Ladders distinguish obstacles from the ground surface.

vertical ladders measure the ground profile in three directions, and reveal that the truck is driving toward the foot of an upward incline. The “long straight feature” is merely a surface contour of the upward-sloping ground, and therefore, since the incline is not too steep, should not be considered an obstacle. The two smaller clusters of returns, however, appear to be at a significant altitude above the notional ground, and are interpreted as nontraversable obstacles. In fact, these are traffic cones.

The entire process is  $O(n)$  in the number of lidar measurements  $n$ , with a large array providing  $O(1)$  access to accumulated obstacle detections in a given location. A many-to-one mapping between latitude-longitude coordinates and cells of the array is needed, with the properties that: (a) Each connected preimage of an array cell is at least approximately the same physical size, and (b) any two distinct regions which are mapped to the same array cell are sufficiently far apart that they will not both need to be considered within the planning horizon of the vehicle. A simple method, which works everywhere except in the immediate vicinity of the poles, is to define a latitude-dependent cell size, so that a different integral number of array cells correspond to a fixed extent of longitude at each latitude. It is acceptable that fewer array cells are needed further from the equator and, therefore, some array cells will have more preimage locations than others. The method could be adjusted to deal with the polar neighborhoods by exception.

Once confirmed, obstacles persist unless and until a period of time (e.g., 1 s) passes with no lidar returns detected from that location, in which case the obstacle expires. This enables the system to recover from false positive detections, and also gives a

rudimentary capability to deal with moving obstacles, since obstacles can disappear from one place and be redetected somewhere else. However, we did not attempt to form any velocity estimate of moving objects, and the robot generally operates on the assumption that other objects have zero velocity in the world frame.

In order to save computational time and memory, we did not wish to track obstacles which were well outside the DGC course boundaries. Off-course obstacles should be irrelevant to the vehicle’s planning problem, and regularly checking to see whether they have expired should be a waste of time. Therefore, nontraversable surfaces off the course were not classified as obstacles, as long as the vehicle itself remained on the course. However, sensor measurements indicating off-course obstacles were allowed to accumulate, so that if the vehicle departed from the course boundaries for any reason, and was required to consider off-course obstacles as significant, these obstacles would pass the confirmation threshold very quickly.

### 3.2. Empirical Lidar Detection Results

The NQE obstacle course provided a uniform test environment with well-defined obstacles, of which many different sensor recordings presumably now exist, so it may be useful to report our lidar classification results during traversals of this obstacle course. The ranges at which the intended obstacles (parked cars, tire stacks, and tank traps) were recognized as nontraversable by the vehicle are shown in Figure 7.

DARPA lined the boundaries of the course with traffic cones—which the vehicle, relying on its own GPS localization measurements, might consider to lie either inside or outside the course boundary. Those traffic cones considered to be on the course were classified as nontraversable at ranges indicated in Figure 8. Of the four outliers on the low end (cones which were not identified until they were within less than 20 m range), two cones were occluded from early view by other objects, and two were at the base of an incline and presumably could not be detected until the vehicle crested the top of the slope and headed down.

There were zero-false negatives. Every intentional obstacle and cone on the course was correctly classified and, once classified, was persistently re-



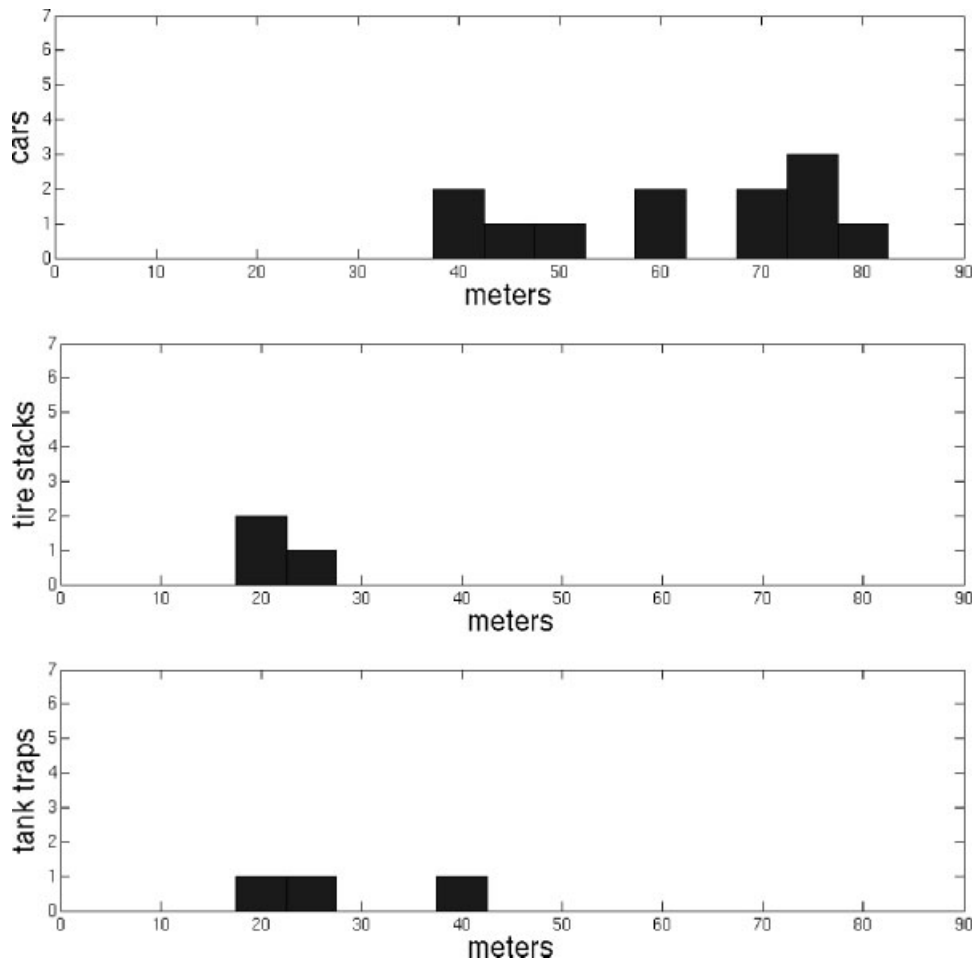


Figure 7. Histograms of NQE obstacles arranged by range of first detection.

garded as an obstacle as long as it remained within the 180° forward sensor arc of the vehicle.

There were, however, a considerable number of false positives, classifying terrain which was traversable as nontraversable. If these false obstacles ap-

peared in the path of the vehicle, the vehicle would of course try to plan a new trajectory around them, and reduce speed if necessary. However, the false obstacles not did persist as the vehicle approached. Instead, all false obstacles eventually expired; leav-

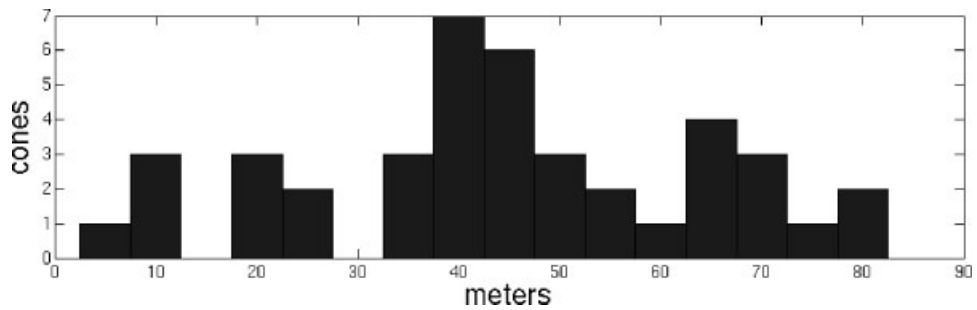
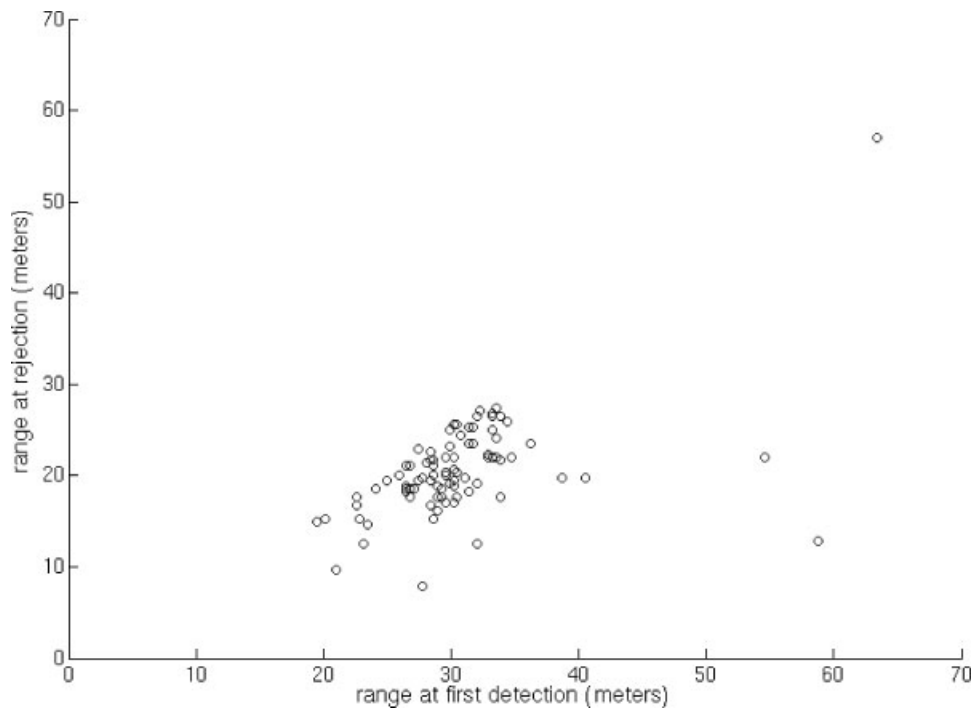


Figure 8. Histogram of NQE traffic cones arranged by range of first detection.



**Figure 9.** False positive events in which obstacles were “detected,” but subsequently rejected.

ing the vehicle free to drive over that terrain. The ranges at which false obstacle detections first appeared and then expired are shown in Figure 9. The mean range at first appearance was 30.5 m; the mean range at expiration was 20.5 m.

Some of the false positives coincided with irregularities in the ground surface, or debris, strewn on the course. In hindsight, it appears likely that a large percentage of the false positives were caused by reflective markings on the edges of the speedway track; causing off-axis reflections of the laser beams and confusing the ladar range measurement. We infer this from the location of the false positives, but have yet to examine the phenomenon through deliberate experiment. Similar problems occurred with reflective road markers during the Grand Challenge Event (GCE).

False positives very seldomly occurred when the vehicle was traveling on a continuous unmarked road surface, e.g., the asphalt track at the NQE, or a dirt road in the GCE. The main NQE performance impact of the false positives was to cause the vehicle to hesitate at transitions crossing the marked edge of the asphalt. However, the vehicle still managed to

maintain a high average speed and complete the obstacle course in competitive times. (See Table I.)

#### 4. AVOIDER

We accomplished vehicle trajectory planning using a custom recursive algorithm described in this section. In keeping with the general philosophical approach of the team, we attempted to design for a minimal computation footprint, taking strategic advantage of heuristic rules and knowledge implicit in the DARPA-provided route definition data file (RDDF) route. The method bears a resemblance to the generation of a probabilistic roadmap (Kavraki, Svestka, Latombe & Overmars, 1996) or a rapidly exploring random tree (Frazzoli, Dahleh & Feron, 2002; LaValle, 1998), in that we generate a graph of vehicle configurations connected by smooth trajectories, but instead of generating new configurations on the boundary of an expanding graph, we recursively generate trajectory midpoints in search of the best feasible path connecting a start configuration and end configuration.

In our search for high efficiency, in practice, we

forfeited any guarantee of the global optimality of our solution paths and even predictable convergence conditions for the routine. However, we found that in the vast majority of cases, traversable paths are rapidly found without burdening the processing resources of the vehicle.

The stage for the planning algorithm is a Cartesian 2D map in the vicinity of the initial global coordinates of the vehicle, populated with a number of discrete obstacles. The obstacles are represented as point hazards that must be avoided by a particular radius, or as line segments that can be crossed in only one direction. Point obstacles are centered on locations in the plane that have been identified as non-traversable by the ladar system. The buffer radius surrounding each point obstacle includes the physical width of the vehicle and, additionally, varies based on the distance from the vehicle to the hazard. A real object, such as a wall or car, is represented by a cluster of such points, each with its associated radius. Line segment obstacles arise from the RDDF, which specifies corridor boundaries for the vehicle. The vehicle trajectory is a single curve describing the motion of the vehicle frame in the plane.

Our task is to find a drivable path from an initial configuration to a destination configuration that does not encroach on any obstacle.<sup>2</sup> The destination is taken to be the center of the RDDF corridor at some distance ahead of our sensor horizon. The simplest and presumably most frequently occurring scenario will require the vehicle to simply drive forward from/to without performing any evasive maneuvers. We represent this scenario with a directed acyclic graph containing two nodes and a single connecting edge. This choice of data structure later allows us to take advantage of a topographically sorted ordering, that enables the least cost traversal of the graph to be found in linear time [ $O(N \text{ edges})$ ]. Each node in the graph is associated with a possible configuration of the vehicle, and each edge is associated with a directed path connecting a starting configuration to a target configuration. At all times, care is taken to maintain the topological correspondence between the nodes in the graph and the locations in the local map.

After initialization we enter the recursive loop of the algorithm, which consists of three stages:

1. Graph Evaluation,

<sup>2</sup>At this time, we have no classification of obstacles by importance. All obstacles are regarded as equally nontraversable and equally to be avoided.



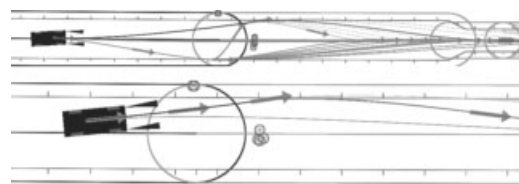
**Figure 10.** Visualization of Avoider algorithm at GCE start line.

2. Path Validation, and
3. Graph Expansion.

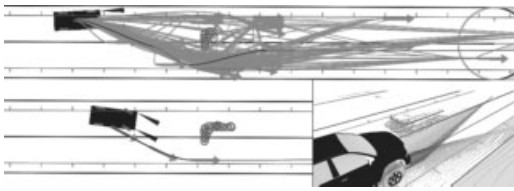
This loop is executed repeatedly until a satisfactory path is found from/to, or until a watchdog termination condition is met. Typically, we would terminate the planner if a path was not found after several hundred milliseconds.

Figures 10–12 offer a visualization of the path planning process. Nodes are indicated by bright purple arrows, while considered trajectories are drawn as purple lines.

In Graph Evaluation, trajectory segments and cost factors are computed for all new edges in the graph. Each trajectory segment is calculated from the endpoint node configurations that it connects, and afterward is checked for possible obstacle collisions. There may be a large number of different trajectory segments to check and a large number of obstacles currently being tracked, bearing in mind that a single real object of any significant horizontal extent will be tracked as a cloud of smaller obstacles which are close together. In order to collision check efficiently, we use a wavefront propagation method to create a map indicating the approximate distance from each point to the nearest obstacle. Once this map is produced, trajectories can be checked rapidly against it for obstacle collisions. If no obstacles are intersected, the cost of traversal is generated from an integral of the instan-



**Figure 11.** Visualization of Avoider graph as the vehicle navigates around a tank trap obstacle during the NQE.



**Figure 12.** Visualization of Avoider graph as the vehicle navigates around a parked car obstacle during the NQE.

taneous curvature along the trajectory. In our experience, the dynamic feasibility of a path can be adequately characterized by this single value.

The loop continues with Path Validation. The optimal path over the entire explored graph is found rapidly by reference to the topological sort of the nodes. If the cost is satisfactory, the loop ends and a refinement procedure begins. This refinement process consists of a number of heuristic modifications that add nodes and edges to the graph to “smooth” calculated trajectories. As a final step, a velocity profile is computed along the solution, so that the vehicle’s speed will be consistent with the curvature of the path and with any DARPA-imposed speed limits. The planning thread then updates the desired trajectory for the steering and velocity feedback control system.

If the total cost of the best graph traversal is too high, we enter the third phase of the algorithm: Graph Expansion. In this stage, edges that intersect obstacles are split at the point where a collision would occur. A number of new nodes are added to the graph for configurations selected according to heuristic avoidance conditions. Unevaluated edges connect these new nodes to the endpoints of the offending trajectory segment. Trajectory segments for these new edges are then computed when the recursive loop begins again with Graph Evaluation.

In the heuristic techniques applied to select good target configurations for obstacle avoidance, the position component of the target configuration is typically projected perpendicularly out from the obstacle or interpolated between the obstacle position and the RDDF boundary. We found that the vehicle heading was similarly best specified as a function of both the heading at the collision point and the RDDF-defined corridor direction.

## 5. VEHICLE STATE ESTIMATION

The path planning and control subsystems of Golem 2 needed a good estimate of the latitude, longitude, heading, and the velocity of the vehicle, at a level of accuracy that was beyond that provided by on-board sensors, such as the C-MIGITS. Two different state estimators were implemented to carry out this task, as a means to provide analytic redundancy. The first state estimator used a model analogous to a bicycle for the vehicle, and relied heavily on the history of state. The second estimator was based on a six-degrees-of-freedom (6DOF) rigid-body model, with the addition of a “soft” nonholonomic constraint on the vehicle’s velocity enforced as a virtual heading measurement.

### 5.1. The Bicycle Estimator

In this section, we will describe the working of the first estimator, henceforward referred to as the bicycle estimator. The bicycle estimator was a discrete time-extended Kalman filter (Gelb, 1974; Kalman, 1960; Kalman & Bucy, 1961; Welch & Bishop, 1995), with the following inputs:

1. Latitude and longitude from a NovAtel GPS sensor at 20 Hz.
2. Rear axle velocity at 30 Hz from a custom Hall sensor system. A set of 16 magnets was installed on the rear axle. Two detectors were attached to the vehicle frame and passed a voltage pulse every time one of the magnets went past them. The two sensors enabled us to have a quadrature encoder, i.e., we were able to distinguish between forward and reverse motion. A discrete-time two-state Kalman filter used the voltage pulses as input and estimated the rate of rotation, which in turn was scaled by the gear ratio and wheel radius to infer the velocity of the vehicle.
3. Steering angle from an absolute encoder at 20 Hz.

The rear axle velocity and steering encoder were used as inputs to the bicycle estimator. The state propagation equations for the bicycle estimator were

$$\tilde{x}_{k+1} = \hat{x}_k + \hat{v}_k \Delta t \frac{\cos(\hat{\phi}_k + \hat{\sigma}_k)}{\cos \hat{\sigma}_k},$$

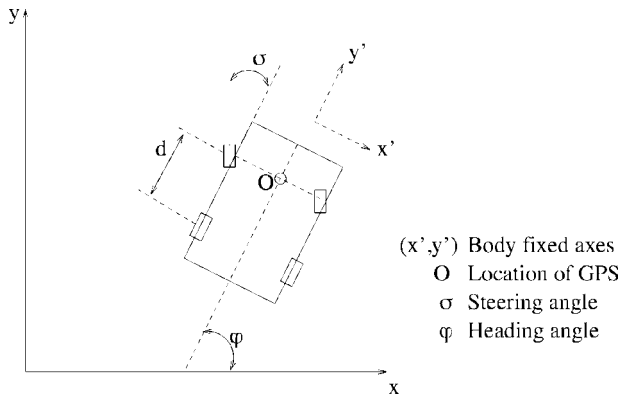


Figure 13. The “bicycle” model.

$$\tilde{y}_{k+1} = \hat{y}_k + \hat{v}_k \Delta t \frac{\sin(\hat{\phi}_k + \hat{\sigma}_k)}{\cos \hat{\sigma}_k},$$

$$\tilde{\phi}_{k+1} = \hat{\phi}_k + \frac{\hat{v}_k \Delta t}{d} \tan \hat{\sigma}_k, \tag{1}$$

where, as described in Figure 13,  $(x, y)$  are the local Cartesian coordinates of the center of the front axle of the car. The GPS sensor is located at this point. The angle  $\phi$  is the heading of the car with respect to the local  $x$  axis. The angle  $\sigma$  is the steering angle of the car as shown in the figure.  $v$  is the rear axle velocity of the car. The quantity  $d$  is the distance between the front and rear axle of the vehicle. A caret over a variable implies that the variable is an estimate, and a tilde over a variable implies that the variable is predicted or propagated forward. The time elapsed since the last state update is  $\Delta t$ . The subscripts in the above equations refer to successive time indices in state propagation.

The bicycle model worked well when the steering angle was small. For large steering angles, however, the model is inaccurate and leads to a considerable lag between the updated state and the GPS measurement. The model was also found to be inaccurate for high velocities, when the vehicle slips at turns. Thus, the steering angle,  $\sigma$ , was calculated as

$$\hat{\sigma}_k = \hat{\gamma}_k (\sigma_{\text{measured}} - \hat{\sigma}_{\text{bias } k}), \tag{2}$$

where  $\gamma$  is the steering calibration factor which tries to compensate for model inaccuracies. The steering

bias estimate  $\sigma_{\text{bias}}$  is used to compensate for bias in the measured steering angle. The rear axle velocity,  $v$ , was calculated as

$$\hat{v}_k = \hat{S}_k (v_{\text{measured}}), \tag{3}$$

where  $v_{\text{measured}}$  is the velocity being input to the bicycle estimator. The slip factor  $S$  compensates for variations in the vehicle’s apparent wheel radius, and for the fact that the vehicle may be going uphill or downhill, and tries to estimate slip. However, the slip factor was not able to track consistently long periods of slipping.

The state variables were latitude, longitude (translated to local Cartesian coordinates  $x, y$ ), heading  $\phi$ , slip factor  $S$ , and either steering bias  $\sigma_{\text{bias}}$  or steering calibration factor  $\gamma$ .

The steering calibration factor  $\gamma$  and the steering bias cannot be estimated simultaneously, as the state variables become unobservable. So, the bicycle estimator was operated in the following two modes:

1. When the vehicle was going straight,  $|\sigma_{\text{measured}}| < 3^\circ$ ,  $\sigma_{\text{bias}}$  was estimated.
2. When the vehicle was turning,  $|\sigma_{\text{measured}}| > 3^\circ$ ,  $\gamma$  was estimated. This enabled compensating for model inaccuracies in hard turns.

### 5.2. The Six-Degrees-of-Freedom Estimator

In this section, we describe the design of the 6DOF estimator. Like the bicycle estimator discussed previously, the 6DOF estimator is implemented as a discrete-time extended Kalman filter. The estimator is designed using fairly standard techniques for strap-down inertial navigation systems. Since a detailed model of the vehicle’s dynamics is not available, the filter relies mainly on the rigid-body kinematic equations. However, due to the absence of a magnetometer or other means to measure the vehicle’s orientation, and the need to be able to ensure convergence of the nonlinear filter without requiring a initial calibration procedures, knowledge of the vehicle’s dynamics is exploited in the form of virtual heading measurements from inertial velocity data.

The vehicle is modeled as a rigid body moving in the 3D space; the state of the vehicle can hence be described by a position vector  $p \in \mathbb{R}^3$ , representing the location with respect to an Earth-fixed reference frame of the on-board IMU, a velocity vector  $v$



$=dp/dt$ , and a rotation matrix  $R \in SO(3)$ , where  $SO(3)$  is known as the Special Orthogonal group in the 3D space, and includes all orthogonal  $3 \times 3$  matrices with a determinant equal to +1. The columns of  $R$  can be thought of as expressing the coordinates of an orthogonal triad rigidly attached to the vehicle's body (body axes).

The inputs to the estimator are the acceleration and angular rate measurements from the IMU, provided at 100 Hz, and the GPS data, provided at about 20 Hz. In addition, the estimator has access to the velocity data from the Hall sensors mounted on the wheels, and to the steering angle measurement.

In the following, we will indicate the acceleration measurements with  $z_a \in \mathbb{R}^3$ , and the angular rate measurements with  $z_g \in \mathbb{R}^3$ . Moreover, we use  $Z_a$  to indicate the unique skew-symmetric matrix, such that  $Z_a v = z_a \times v$ , for all  $v \in \mathbb{R}^3$ . A similar convention will be used for  $z_g$  and other 3D vectors throughout this section.

The IMU accelerometers measure the vehicle's inertial acceleration, measured in body-fixed coordinates, minus the gravity acceleration; in other words,

$$z_a = R^T(a - g) + n_a,$$

where  $a$  and  $g$  are, respectively, the vehicle's acceleration, and gravity acceleration in the inertial frame, and  $n_a$  is an additive, white Gaussian measurement noise. Since the C-MIGITS IMU estimates accelerometer biases, and outputs corrected measurements, we consider  $n_a$  as a zero-mean noise.

The IMU solid-state rate sensors measure the vehicle's angular velocity, in body axes. In other words,

$$z_g = \omega + n_g,$$

where  $\omega$  is the vehicle's angular velocity (in body axes), and  $n_g$  is an additive, white Gaussian measurement noise. As in the case of acceleration measurements,  $n_g$  is assumed to be unbiased.

The kinematics of the vehicle are described by the equations

$$\dot{p} = v,$$

$$\dot{v} = a,$$

$$\dot{R} = R\Omega, \tag{4}$$

where  $\Omega$  is the skew-symmetric matrix corresponding to the angular velocity  $\omega$ , and we ignored the Coriolis terms for simplicity. As a matter of fact, this is justified in our application due to the low speed, relatively short range, and to the fact that errors induced by vibrations and irregularities in the terrain are dominant with respect to the errors induced by ignoring the Coriolis acceleration terms.

We propagate the estimate of the state of the vehicle using the following continuous-time model, in which the hat indicates estimates:

$$\dot{\hat{p}} = \hat{v},$$

$$\dot{\hat{v}} = \hat{R}z_a + g,$$

$$\dot{\hat{R}} = \hat{R}Z_g. \tag{5}$$

An exact time discretization of the above, under the assumption that the (inertial) acceleration and angular velocity are constant during the sampling time, is

$$p^+ = p + v\Delta t + \frac{1}{2}(\hat{R}z_a + g)\Delta t^2,$$

$$v^+ = v + (\hat{R}z_a + g)\Delta t,$$

$$R^+ = R \exp(Z_g\Delta t). \tag{6}$$

The matrix exponential appearing in the attitude propagation equation can be computed using Rodrigues' formula. Given a skew-symmetric  $3 \times 3$  matrix  $M$ , write it as the product  $M = \Omega\theta$ , such that  $\Omega$  is the skew-symmetric matrix corresponding to a unit vector  $\omega$ ; then

$$\exp(M) = \exp(\Omega\theta) = I + \Omega \sin \theta + \Omega^2(1 - \cos \theta). \tag{7}$$

The error in the state estimate is modeled as a nine-dimensional vector  $\delta x = (\delta p, \delta v, \delta \phi)$ , where

$$p = \hat{p} + \delta p,$$

$$v = \hat{v} + \delta v,$$

$$R = \hat{R} \exp(\delta\Phi). \tag{8}$$

Note that the components of the vector  $\delta\phi$  can be understood as the elementary rotation angles about the body-fixed axes that make  $\hat{R}$  coincide with  $R$ ; such a rotation, representing the attitude error, can also be written as  $\delta R = \exp(\delta\Phi) = \hat{R}^T R$ .

The linearized error dynamics are written as follows:

$$\frac{d}{dt} \delta x = A \delta x + F n, \tag{9}$$

where

$$A := \begin{bmatrix} 0 & I & 0 \\ 0 & 0 & -RZ_a \\ 0 & 0 & -Z_g \end{bmatrix}, \quad F := \begin{bmatrix} 0 & 0 \\ R & 0 \\ 0 & I \end{bmatrix}. \tag{10}$$

When no GPS information is available, the estimation error covariance matrix  $P := E[\delta x(\delta x)^T]$  is propagated through numerical integration of the ordinary differential equation

$$\frac{d}{dt} P = AP + PA^T + FQF^T.$$

Position data from the GPS are used to update the error covariance matrix and the state estimate. The measurement equation is simply  $z_{\text{GPS}} = p + n_{\text{GPS}}$ . In order to avoid numerical instability, we use the UD-factorization method described in Rogers (2003) to update the error covariance matrix and to compute the filter gain  $K$ .

Since the vehicle’s heading is not observable solely from GPS data, and we wished to reduce the calibration and initialization procedures to a minimum (e.g., to allow for seamless resets of the filter during the race), we impose a soft constraint on the heading through a virtual measurement of the inertial velocity, of the form

$$z_{\text{NHC}} = \arctan\left(\frac{v_{\text{East}}}{v_{\text{North}}}\right) - \lambda \sigma,$$

where  $\sigma$  is the measured steering angle, and  $\lambda$  is a factor accounting for the fact that the origin of the body reference frame is not on the steering axle.

In other words, we effectively impose a non-holonomic constraint (NHC) on the motion of the vehicle through a limited-sideslip assumption. This assumption is usually satisfied when the vehicle is traveling straight, but may not be satisfied during turns. Moreover, when the vehicle is moving very slowly, the direction of the velocity is difficult to estimate, as the magnitude of the velocity vector is dominated by the estimation error. Hence, the virtual measurement is applied only when the steering angle is less than  $10^\circ$ , and the vehicle’s speed is at least 2.5 mph (both values were determined empirically).

The filter described in this section performed satisfactorily in our tests and during the DGC race, providing the on-board control algorithms with position and heading estimates that were nominally within 10 cm and  $0.1^\circ$ , respectively.

### 5.3. Modeling System Noise

The state was propagated and updated every time a GPS signal arrived. There was no noise associated with the state propagation equation (1). It was assumed that there was additive white Gaussian noise associated with the inputs ( $v_{\text{measured}}$  and  $\sigma_{\text{measured}}$  for the bicycle model, and  $z_a$  and  $z_g$  for the six-degrees-of-freedom model). To efficiently track the constants in the state variables ( $S, \sigma_{\text{bias}}, \gamma$ ), it was assumed that there was an additive white Gaussian noise term in their propagation. It was also assumed that the GPS measurement (latitude and longitude) had some noise associated with it. The variances assigned to the noise processes described above were tuned to ensure that the innovations<sup>3</sup> were uncorrelated, and that the estimator was stable, and converged reasonably quickly. By tuning the variances, we can alter the “trust” associated with the history of the vehicle state or with the GPS measurement.

<sup>3</sup>Innovation of a measured data is the difference between the estimated and the measured data.

### 5.3.1. Determining the Appropriate GPS Measurement Noise Variance

The received data from the GPS consisted of the latitude, longitude, and a horizontal dilution of precision (HDOP) value. HDOP is a figure of merit for the GPS measurement, which is directly related to the number of satellites visible to the GPS antenna. The HDOP value is related to the noise in each measurement. However, our attempts at mapping the HDOP values to actual variances were futile, as we did not observe a monotonic relationship. It was noticed that an HDOP of more than 5 usually corresponded to multipath reception in GPS, and consequently, the GPS had an abnormally huge variance in that case. In the absence of any *ad hoc* relationship between the HDOP and noise variance, we opted to keep a constant variance associated with GPS noise if the HDOP was less than 5 and a huge variance otherwise. Also, we noticed that the GPS noise was highly correlated and not white.

### 5.3.2. Projection of the Innovations

The bicycle estimator is based on a very intuitive model of the vehicle, which motivates us to consider the GPS innovations in a physically relevant reference frame, rather than any arbitrary reference frame. It is insightful to project the innovations into the local frame of the vehicle: Parallel to the heading direction and perpendicular to it. The parallel and perpendicular body fixed axes are indicated in Figure 13.

For an ideal estimator, the innovations will be uncorrelated with each other. However, we tuned the estimator to just achieve innovations with zero mean. While tuning the estimator, it was very useful to consider the parallel and perpendicular innovations. For example, a direct current bias in the parallel innovations implied that we were not tracking the slip factor ( $S$ ) adequately. Thus, to ensure a zero-mean parallel innovation, the variance associated with the propagation of slip factor should be increased.

### 5.3.3. Adaptive Shaping of the Innovations

The noise in the GPS data was highly correlated, and there was very little *a priori* knowledge of the variance. Very often, especially when the vehicle would drive near a wall or approach a tunnel, there would be highly erratic jumps in the GPS measurements

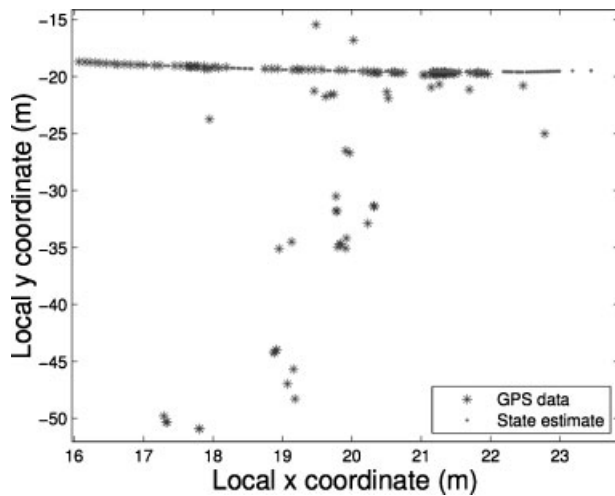
due to multipath reflections. Without any *a priori* knowledge of the variance in such cases, the state estimate would bounce around a lot. This was undesirable as it would hamper the path planner and the obstacle detection subroutines in the main program.

To counter these “unphysical” jumps, once the estimator was converged, the innovations were clipped up to a certain maximum absolute value. For example, a GPS measurement corresponding to a perpendicular innovation of 2 m in 0.05 s while going straight is unphysical, and so perpendicular innovation should be clipped to a nominal value (in our case, 6 in.). This prevented large jumps in state estimate, but had a grave disadvantage. It was observed that if the innovations were clipped to a fixed range, then in certain situations, the state estimate will lag far behind from a “good” set of GPS measurements, and take a long time to converge back. To prevent this from happening, the clipping limit of the innovations was determined adaptively as the minimum of either a fixed limit, or the mean of the innovations in the last 2 s scaled by a numerical factor slightly greater than unity. The parallel and perpendicular components of the innovation were clipped separately with different numerical constants used.

### 5.3.4. Countering the Time Delays

There was some finite delay between the appearance of sensor data on the bus and the time they were processed by the control program. Usually, this delay was nominal ( $\sim 50\text{--}200\ \mu\text{s}$ ), but it was sporadically very large. A large delay in GPS data manifested in large negative parallel innovation. However, the large innovation was clipped effectively by the method described earlier, and consequently did not effect the state estimate. In the future, we plan to implement a routine which synchronizes the time between all the serial/USB data sources.

Performance of the state estimator while going under a bridge is shown in Figure 14. “\*” represents the GPS data received in a local Cartesian coordinate system. “.” represents the estimated location of the truck. Golem 2 was moving from left to right in this figure. Note that the GPS data have a huge variance due to the multipath. Also note that the GPS noise is highly correlated; in this case, the variance is huge in the direction perpendicular to the motion as compared to the parallel direction. As seen from the fig-



**Figure 14.** Performance of state estimator while going under a bridge.

ure, the performance of the state estimator is immune to the large unphysical jumps in GPS data. Occasional jumps of length  $\sim 0.3$  m are observed in the successive updates of estimated state. These correspond to a delay in received GPS data and large negative parallel innovations, as discussed in this section.

### 5.3.5. Special Modes of Operation

There were a couple of situations that required special handling instructions:

- The GPS signal was observed to drift considerably when the vehicle was at rest. Not only was this unphysical, but it is also detrimental to path planning. Thus, when the vehicle was going considerably slowly or was at rest, the variance assigned to the GPS measurements was increased significantly. In such a case, the bicycle estimator essentially worked as an integrator, rather than a filter.
- It was observed that the GPS signal would occasionally jump discretely. These jumps usually corresponded to the presence of a power transmission line nearby. The difficulty was that the GPS took a while ( $>2$  s) to reconverge after the jumps. These unphysical jumps were easily detected from the jumps in the parallel and perpendicular innovations.

After the detection of such jumps, the GPS variance was increased until it was trustworthy again, i.e., until the innovations were within a certain limit again.

### 5.3.6. Initialization of the IMU

One advantage of this model was that it converged very fast while going straight, usually in approximately 5 s. Once the bicycle model converged, the heading estimate was used to initialize the IMU. While going straight, the performance of the bicycle estimator was extremely good as the heading estimate was within  $0.5^\circ$  of the IMU-computed heading. However, on sharp turns, the heading estimate was up to  $\sim 3^\circ$  from the IMU-computed heading. Thus, the IMU-computed heading was given more importance, especially when GPS signals were bad. In the future, we plan to extend the bicycle model to include the angular rotation and linear displacement data from the IMU.

## 6. VISION SYSTEMS

For computer vision, desert paths present a different challenge from paved roads, as the environment is far less structured, and less prior information is available to exploit in constructing algorithms. Our approach was to integrate existing vision technologies which have been proven to work on-road but have the potential to be transferred to the off-road domain. These include learning-based road-finding and binocular stereo reconstruction.

### 6.1. Mobileye Vision System

Golem 2 was equipped with a sophisticated vision system, created by Mobileye Vision Technologies Ltd., consisting of a single camera and a dedicated processing unit. On-road, the Mobileye system can find lane boundaries and detect other vehicles and their positions in real time. The system was adapted to the off-road environment by Mobileye and the Hebrew University of Jerusalem.

The Mobileye system combines region-based and boundary-based approaches to find path position and orientation relative to the vehicle. The two approaches complement each other; thus allowing reliable path detection under a wide range of cir-



cumstances. Specifically, we use a variety of texture filters together with a learning-by-examples AdaBoost (Freund & Schapire, 1996) classification engine to form an initial image segmentation into path and nonpath image blocks. In parallel, we use the same filters to define candidate texture boundaries and a projection-warp search over the space of possible pitch and yaw parameters, in order to select a pair of boundary lines that are consistent with the texture gradients and the geometric model. Both the area-based and boundary-based models are then combined (weighted by their confidence values) to form a final path model for each frame.

#### 6.1.1. Region-Based Path Detection

The gray-level image is divided into partially overlapping blocks. A filter bank is applied to all image pixels and a descriptor vector is generated per block. The descriptor contains the mean and standard deviation of the filter response over the block for each of the 16 filters. Each entry in the texture descriptor can be considered as a “weak” learner, in the sense that it forms class discrimination. The iterative AdaBoost algorithm combines the weak learners to form a powerful classification engine that assigns a *path* or *nonpath* label to every block according to the training data. The training data were extracted from 200 images that were gathered on various parts of the 2004 Grand Challenge route. The block classification by itself is not sufficient for autonomous vehicle path planning, because about 10% of the blocks are expected to be misclassified. Filtering methods are used to clear some of the misclassified blocks, followed by detection of path boundaries. The path boundaries are derived via a minimal error separating line on each side of the path. The system confidence is calculated from the separation quality and the sensing range (the distance to the farthest point that we can reliably identify as the path). Figure 15 shows the results of each of the main parts of the algorithm.

#### 6.1.2. Boundary-Based Path Detection

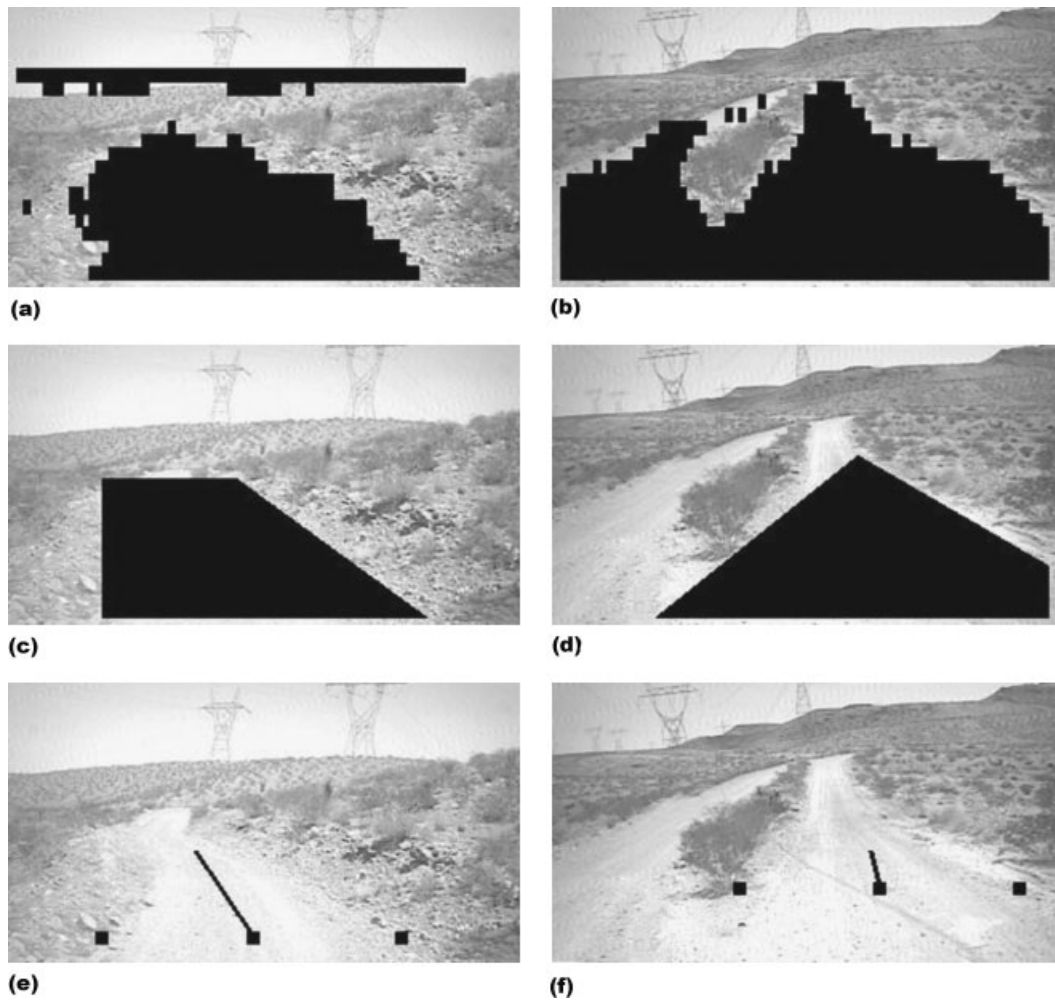
The boundary-based technique does not rely on prior learned texture information. Instead, it makes the assumption that the path texture properties are different than the surrounding nondrivable areas. For this cue to be reliable, we have to constrain the solution to a strict geometric model, where the path

boundaries lie on straight parallel edges. This allows us to reduce the problem of finding a drivable path to four degrees of freedom:  $(x, y)$  position of the vanishing point, and left and right distance to the edge of the path. The geometric constraints resulting from assuming a flat world, perspective camera, and parallel path boundaries in the world suggest the following projection-warp scheme per frame: Given a hypothesis of pitch and yaw angles of the camera, the image is warped to form a top view in world coordinates. In the warped image, the path boundaries are supposed to be *parallel* vertical lines if indeed the pitch and yaw angles are correct. A projection of the image texture edges onto the horizontal axis will produce a one-dimensional (1D) profile whose peaks correspond to vertical texture edges in the warped image. We look for a pair of dominant peaks in the 1D profile, and generate a score value which is then maximized by search over the pitch and yaw angles via iterating the projection-warp procedure just described. The search starts with the pitch and yaw angle estimates of the previous frame, followed by an incremental pitch and yaw estimation using optic-flow and a small motion model:

$$xw_x + yw_y = yu - xv, \quad (11)$$

where  $(u, v)$  are the flow (displacements) of the point  $(x, y)$  and  $w_x, w_y$  are the pitch and yaw angles. The warped image is divided into overlapping  $10 \times 10$  blocks with each pixel forming a block center. Using the same filter bank as in the region-based method, we estimate the likelihood,  $e^{-\Delta}$ , that the vertical line passing through the block center forms a texture gradient, where  $\Delta$  is the  $L_1$  distance between the texture vector descriptors of the two respective halves of the block. To check a hypothesis (for pitch and yaw), we project the horizontal texture gradients vertically onto the  $x$  axis and look for peaks in this projection. An example result of this projection is shown in Figure 16(d). The path boundaries and other vertical elements in the image create high areas in the projection, while low areas are most likely caused by vertical texture gradients that are not continuous and created by bushes, rocks, etc. The peaks in this projection are maximized when the vanishing point hypothesis is correct and the path edges (and possibly other parallel features) line up. By finding the highest peaks for these hypothesis, our system is able to find the lateral position of the left and right





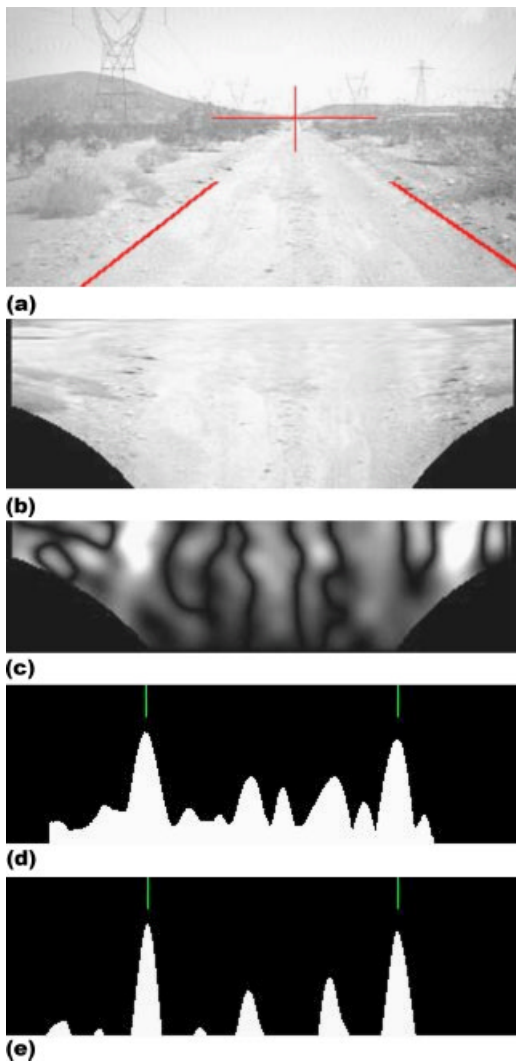
**Figure 15.** In (a) and (d), blocks are classified by texture into *path* or *nonpath*. In (b) and (e), sky blocks are removed and three lines, arranged in a trapezoid, are fitted to the *path* blocks. The trapezoid is considered to represent the path. Finally, in (c) and (f), the path boundaries are calculated at a given distance ahead of the vehicle (5 m, in this example) together with the path center and heading angle.

boundaries. Figure 16(e) shows the “cleaned-up” 1D projection profile and the associated pair of peaks corresponding to the path boundary lines.

### 6.1.3. Performance

The system was implemented on a Power-PC PPC7467 1 GHz running at 20 frames per second. The camera was mounted on a pole connected to the front bumper (Figure 17) to allow maximal field of view. We tried both 45° and 80° field of view lenses, and found the latter to be more suitable for auto-

nomous driving, where the vehicle is not necessarily centered over the path. For our applications, the most meaningful overall system performance measure is to count how often (what fraction of frames) the system produced correct path edge positions and, where appropriate, heading angles. Furthermore, it is crucial for the system to know when it cannot determine the path accurately, so that the vehicle can slow down and rely more on information from the other sensors. Our results are broken up by different terrain types. For each, representative challenging clips of 1000 frames were selected, and the



**Figure 16.** Projection-warp search: (a) Original image with the overlaid path boundary and focus of expansion results, (b) the warped image, (c) texture gradients magnitude, (d) projection: Vertical sum of gradients, and (e) projection profile followed by convolution with a box filter. The two lines on top of the histogram mark the path boundaries.

system performance scored, on these sequences by a human observer. The path edge distance accuracy was computed by observing the position of the road edge marks approximately 6 m in front of the vehicle. A frame was labeled incorrect if the path edge marker at that location appeared to be more than 30 cm ( $\approx 18$  pixels) away from the actual path boundary. For straight paths, the perceived vanish-



**Figure 17.** The camera is mounted inside a housing, atop a pole connected to the front bumper. This allows a better field of view than mounting the camera on the windshield.

ing point of the path was also marked, and our algorithm's heading indicator was compared to the lateral position of this point.

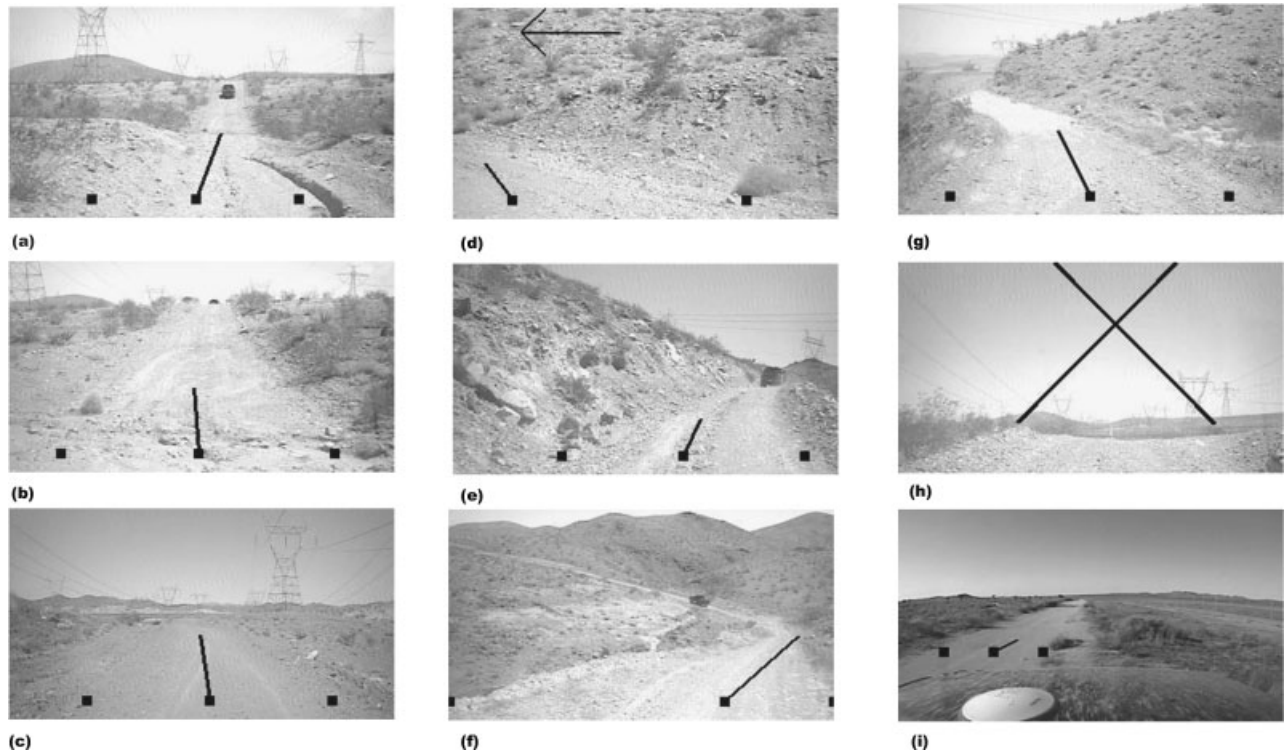
On relatively straight segments with a comfortably wide path, our system reported availability (high system confidence) 100% of the time, while producing accurate path boundary locations 99.5% of the time. The mean angular deviation of the heading angle from the human marked vanishing point was  $1.7^\circ$ .

The second test clip is an example of more uneven terrains with elevation changes. Here, the vehicle passes through a dry river ditch [Figure 18(b)], where both the path texture and scene geometry are difficult. When our vehicle is reaching the crest of the hill [Figure 18(h)], only a short segment of road is visible. In this case, the system reported unavailability (low confidence) 8% of the time. When available, however, the accuracy in boundary locations was 98%.

The final clip contains a winding mountain pass [Figure 18(g)]; difficult due to path curvature as well as texture variation. Despite these, our system was available throughout the clip, and achieved an accuracy of 96% in detecting the path boundary.

#### 6.1.4. Integration

The combination of the learning and geometric approaches yields high-quality results with confidence estimates suitable for integration into our control systems. Output from the Mobileye system—which



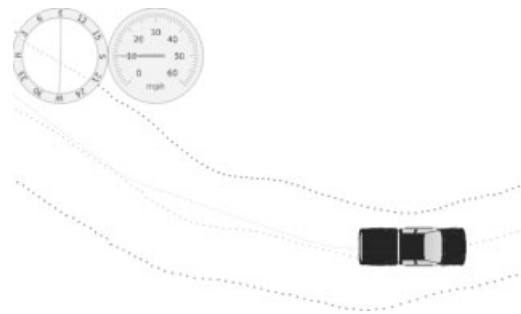
**Figure 18.** Sample images and system output from 6 h of driving in the Mojave desert. The path is marked by two left-right boundary points and a center point with heading orientation. The “X” mark in (h) coincides with zero confidence due to short range of visible path. In (i), the path is detected even though the vehicle is not centered on the path (a common situation in autonomous driving).

included path boundaries, orientations, and pitch—was integrated into the Golem path planner. Path boundaries were marked as line obstacles, and projected onto the world coordinate frame using the known transformation between the Mobileye camera, the GPS antenna, and the road surface. Figure 19 shows the detected trail boundary and trail center relative to the vehicle and to the vehicle’s actual trajectory.

### 6.2. Toshiba Stereo Vision System

The Golem/UCLA Team experimented with a variety of stereo vision systems for the purposes of obstacle detection, ground-plane registration, and path finding. Fixed-camera stereo is a well-studied problem, and there are a number of academic and commercial systems of varying quality. Long-range sensing is essential for use in a high-speed automobile, since time is of the essence; it is impractical and

sometimes impossible to stop to analyze nearby obstacles. This requirement translates into a wide baseline separating the stereo cameras, since the maximum range of the system is determined by this distance. A further performance constraint is pro-



**Figure 19.** Trail boundaries detected by the Mobileye system.



Figure 20. Setup of stereo cameras.

cessing time, since latency can introduce dangerous errors in path planning and control. Toshiba Research, in Kawasaki, Japan, developed a stereo system for on-road driving at high speeds, which we installed on Golem 2. Due to insufficient time, we did not integrate the stereo system into the control system of the vehicle before the GCE, but there is no doubt that it has a high potential for successful autonomous driving. In this section, we describe the hardware configuration and implementation details.

6.2.1. Hardware Configuration

Figure 20 shows the setup of our stereo cameras. Two metal plates sandwich and rigidly fix the cameras, so that they can withstand the strong vibrations caused by off-road driving. The distance between the two cameras is 1.2 m, and each camera is about 1.5 m above the ground plane. We use charge coupled device (CCD) cameras with 7.5 mm lenses that have an image resolution of  $320 \times 240$  pixels.

Our stereo system is based on a multi-VLIW (very long instruction word) processor called *Visconti* (Hattori & Takeda, 2005; Tanabe, 2003). The processor architecture is designed to ensure efficient

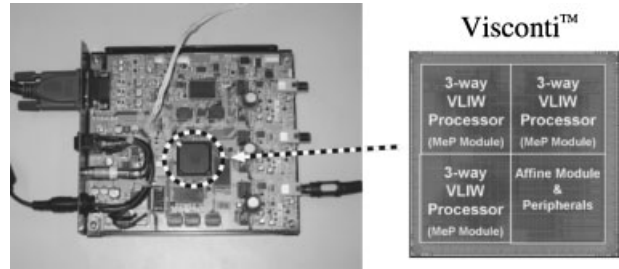


Figure 21. Prototype processing hardware.

performance for general image processing operations, while satisfying several requirements for automotive use, e.g., operating temperature range of  $-40$ – $+85^\circ\text{C}$ , power consumption  $<1\text{ W}@150\text{ MHz}$ . Figure 21 shows a prototype of an image processing unit using Visconti. It has three video input channels and a video graphics array video output to display the processing results. Figure 22 shows the block diagram of Visconti. The processor includes one image transformation module and three processing modules operating in parallel. Each of the three processing modules consists of a reduced instruction set computer processor core and a VLIW coprocessor. Several types of single-instruction multiple-data (SIMD) operations required for stereo computation, including convolution, accumulation, and pixel shift, are supported in the instruction set of the coprocessor. Each processing module also has a scratch pad memory and a direct memory access controller,

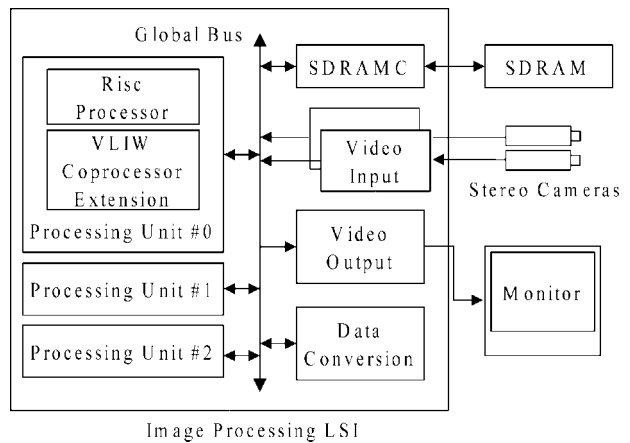


Figure 22. Block diagram of Visconti.



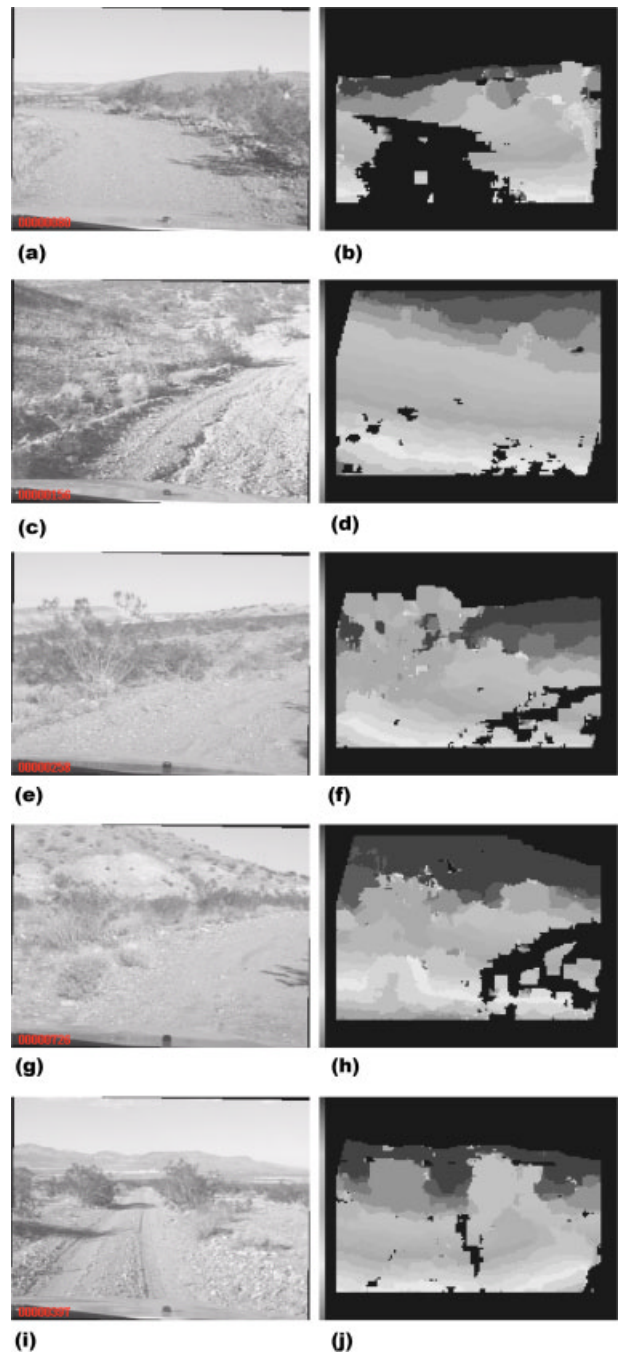
so that memory access latency is hidden by double-buffering data translation.

### 6.3. Implementation Details

We adopt the sum of absolute differences (SAD) as a matching criterion within a  $7 \times 7$  window, as SAD is less computationally expensive than other measures such as the sum of squared differences and normalized cross correlation. We also use a recursive technique for the efficient estimation of SAD measures (Faugeras et al., 1993; Hattori & Takeda, 2005). In order to compensate for possible gray-level variations due to different settings of the stereo cameras, the input stereo images are normalized by subtraction of the mean values of the intensities within a matching window at each pixel. Also, the variance of intensities at each point is computed on the reference image to identify those regions which have insufficient intensity variations for establishing reliable correspondences.

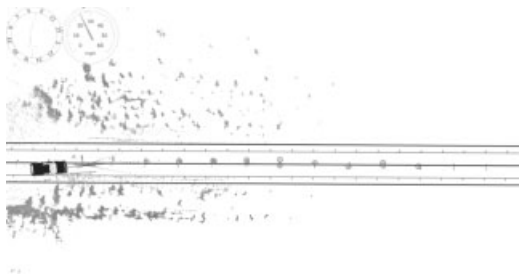
As Visconti has one image transformation module and three processing modules operating in parallel, task allocation for these modules is crucial to real-time operation. For instance, the stereo rectification is an indispensable process that transforms input stereo images so that the epipolar lines are aligned with the image scan lines. The image transformation module carries out the stereo rectification, which is difficult to accelerate by SIMD operations due to irregular memory access. Also, we divide a pair of images into three horizontal bands which are allocated to those three processing modules. Each of three areas has about the same number of pixels, so that the computation cost is equally distributed across the three modules.

Due to the recursive technique for SAD computation, those task allocations, and SIMD instructions, our stereo system is capable of disparity estimation at a rate of about 30 frames/s with up to 30 disparity levels and an image input size of  $320 \times 240$  pixels. This performance is higher than that of a 2.0 GHz processor with SIMD instructions. Figure 23 shows several examples of disparity images. More red intensity indicates larger disparity values which means closer areas, while black indicates textureless regions. The bottom of input images is excluded from the stereo computation since it corresponds to a part of the hood of the vehicle. These input stereo images were taken in the Mojave desert.



**Figure 23.** Input images and their disparity maps. More red intensity indicates larger disparity values, i.e., closer regions, and black indicates textureless regions. Note that a part of the hood of the vehicle appears on the bottom of input images, and these regions are excluded for the disparity estimation.





**Figure 24.** Golem 2 misperceives reflective dots on a paved road surface as obstacles.

## 7. RESULTS

Golem 2's qualifying runs on the NQE obstacle course were among the best of the field, as shown in Table I, although we also failed on two runs for reasons discussed in Section 7.1.

Golem 2 raced out of the start chute at the 2005 GCE in the seventh pole position. We knew that Golem 2 was capable of driving well at high speeds. Our speed strategy was that the vehicle would drive at the maximum allowed speed whenever this was below 25 mph. If the recommended speed was greater than 25 mph (implying that the maximum allowed speed was 50 mph), then Golem 2 would exceed the recommended speed, by small amounts at first, but more and more aggressively as the race continued, until it was always driving at the maximum legal speed, except, of course, when modulating its speed during a turn.

As expected, Golem 2 made rapid time on dirt roads and over a dry lakebed. On a paved bridge, Golem 2's laser sensors misperceived the reflective "Botts' dots" in the center of the road as obstacles, which seemed to vanish like a mirage as the vehicle got closer. (See Figure 24.) This caused the vehicle to weave back and forth on the bridge, alarming the DARPA observers in the chase vehicle. But our vehicle kept going and once it reached dirt road again, it straightened out and resumed progress at over 30 miles per hour.

The DARPA observers characterized Golem 2 as initially "skittish" and compared it to a teenage driver, but stated that once it left the paved road and entered the desert, they were impressed by its performance and believed they had a winner on their hands.

Unfortunately, after driving 22 miles in just un-

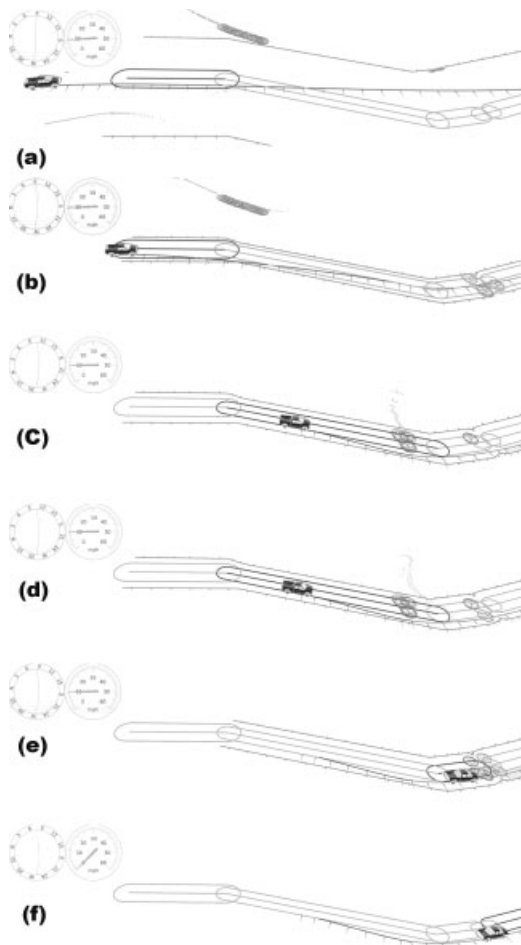
der 1 h, the computer crashed due to faulty memory management. The uncontrolled vehicle departed from the course boundaries at high speed, crashing through vegetation. The DARPA "pause" button was no longer functional, since no software was running, and the DARPA observers did not press the "disable" button in case the vehicle might recover. Golem 2 hurtled more than one-half mile off the course before the pounding from the rough terrain finally shook connectors free from its fusebox, killing the engine.

### 7.1. Causes of Failure

Golem 2 crashed on three significant occasions: Twice during NQE trials and once during the GCE. We think that all of these failures should be considered mere "bugs" rather than fundamental flaws in the design. Nevertheless, it may be interesting to review the causes of these failures.

On its first attempt at the NQE course, Golem 2 immediately veered off to the right and crashed into one side of a gate intended to simulate a cattle crossing. It knocked down the fence beside the gate and came to a stop. The primary cause of this failure was that one of the vertical ladars had been repositioned and miscalibrated (due to a missing decimal point). Mishandling of the course start conditions was a contributing factor.

The sequence of events is illustrated in Figure 25. At the 2005 NQE, vehicles were launched out of start chutes which were located far outside the designated course boundaries. We should have been prepared for this special case and the correct procedure was to consider the course boundaries to extend backward to the start position. However, instead Golem 2 reacted as it would generically react to being far off course, by relaxing the course boundary constraints outward. In Figure 25(a), the vehicle is moving in a straight trajectory, which is hardly constrained by the course boundaries. In Figure 25(b), the vehicle has moved back onto the RDDF course, and also detected the gate ahead, where the orange circles indicate obstacles. The planning boundary constraints have contracted inward and the vehicle has planned a trajectory which is very nearly correct, i.e., a trajectory which passes through the first gate. Unfortunately, the boundary constraints have not tightened quite enough and the trajectory skirts the right edge of the RDDF course. In Figure 25(c), because of the miscalibrated ladar, the vehicle has misperceived a cloud of phantom ob-



**Figure 25.** An initial failure of Golem 2.

stacles where no obstacles actually existed, and planned to swerve around them to the right. In Figure 25(d), the vehicle has perceived that its new trajectory collides with a real obstacle, the fence, but it cannot find a plan that does not appear to result in collision. In Figure 25(e), collision is imminent and the vehicle belatedly attempts to brake. In Figure 25(f), the fence has been knocked down and the vehicle has come to a stop. Although the vehicle was physically capable of proceeding forward over the crushed fence, there was no “restart” logic enabling the vehicle to begin moving again.

Our reaction to this failure was, of course, to fix the calibration of the vertical ladar, to correctly handle the special case of starting outside the course boundaries, to improve the reaction of the velocity

controller to obstacles, and to prevent the vehicle from coming to a permanent stop if not paused. We were able to carry out these fixes only because of the very useful dashboard visualization tool, shown in Figure 25 and elsewhere, that enabled us to closely examine the results of the failed run and simulate what would result from changes to the software.

After two very successful completions of the NQE course, Golem 2 crashed again on the fourth attempt. This time, the bug was in the path planner, which failed to properly validate all the possible candidate trajectories and ended up selecting a degenerate trajectory containing two sharp 180° turns. The impossibly tight loop in the desired trajectory caused the vehicle to jerk suddenly into a concrete barrier. This event motivated increased evaluation of candidate trajectories, and repair and reinforcement of Golem 2’s steering actuator.

Golem 2’s final and most distressing failure occurred during the GCE due to static memory over-allocation. Large amounts of random access memory were set aside at start time for use in recording obstacles, trajectories, and sensor history. In fact, the memory was overallocated, but this did not become apparent until a large sensor history had accumulated, which, because of the mapping between geographic coordinates and elements of the sensor observation array, only occurred when a large amount of terrain had been covered. Golem 2 had made experimental autonomous runs of 10 miles or so, but had never made a continuous overland journey on the scale of the GCE. Furthermore, an endurance trial which consisted of driving for long periods around a track would probably not have uncovered this bug. Only when Golem 2 had driven across 22 miles of new terrain did the memory bug manifest itself and crash the control program.

Although the Golem 2 software is inherently memory intensive in its approach, it should be able to operate with well under 1 GB of random access memory, and therefore this failure was perfectly avoidable in principle.

## 8. SUMMARY AND FUTURE WORK

Despite occasional problems, the Golem vehicles have demonstrated a high level of high-speed driving performance, and we think that our design approach has promise. The system managed to negotiate ob-

stacles at speed using a relatively small amount of computational power (a single 2.2 GHz laptop) and relatively sparse laser range data.

The key drivers of this economically promising performance include a simplified computational architecture; using a combination of horizontally and vertically oriented ladars to reliably sense major obstacles while disregarding inessential details of the terrain; a fast heuristic planner which rapidly finds solutions in typical driving situations; and vehicle state estimation using both an IMU and physical reasoning about the constraints of the vehicle.

The “false” obstacles sometimes announced by the ladar system were not entirely spurious, but generally represented road markings or minor traversable obstacles. Ideally, these would neither be ignored nor mistaken for nontraversable obstacles, but placed in a third category and treated appropriately by the planning software. A future direction for the sensing software is to improve the handling of these features, and also to improve the handling of moving obstacles.

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